

Wealth Optimization

Risk, Return, Goals and Liquidity Through an Investors Lifecycle



AR
IPM Quant Bootcamp®

Dr. Dan Rosen

July 20th 2023

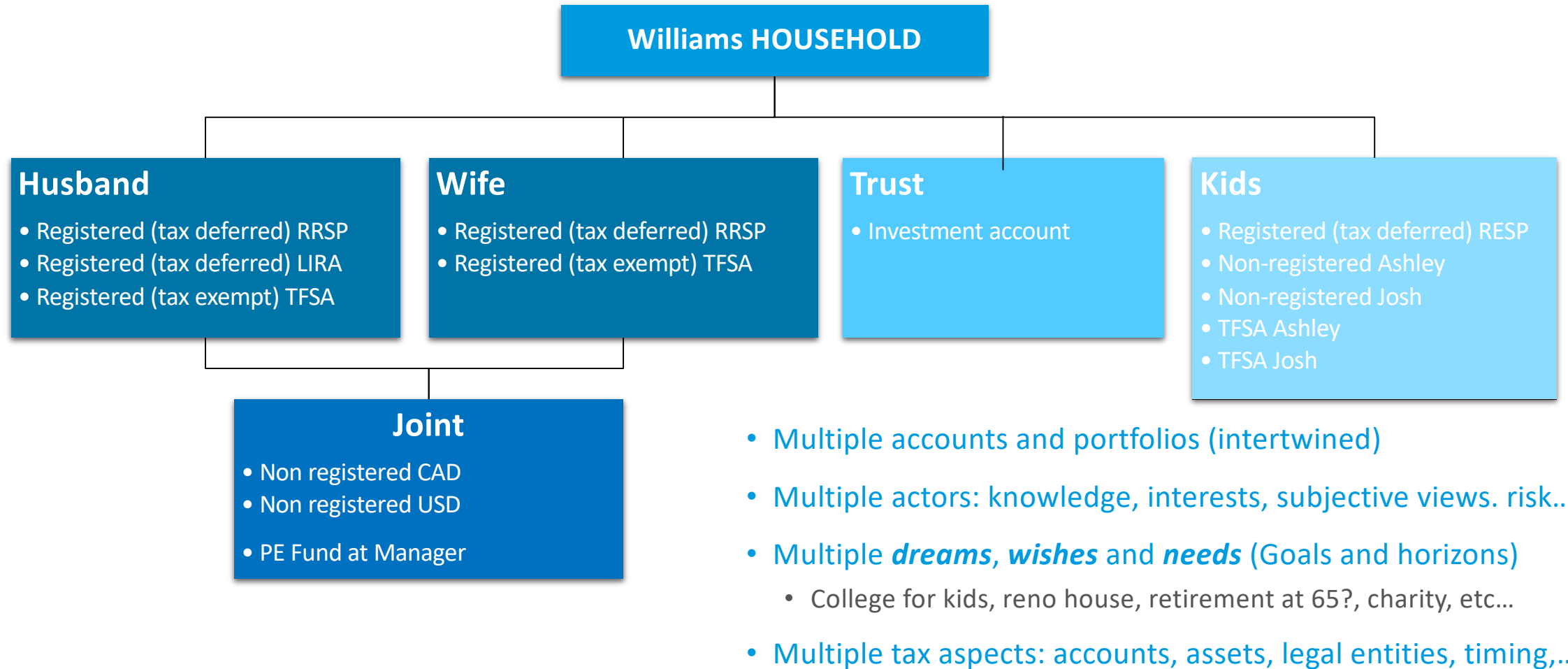




Optimization in Wealth Management

Creating Robots or Empowering Advisors?

It All Starts with a Client/Family



In Practice... Financial Advice... for *Humans*

The actual problem is very complex!

Financial Advisors work with *people* (individuals, families) with human goals, feeling, fears, and (*not so rational*) reactions... and in the real (complex financial) world

- Truly hard to define precisely the problem to optimize (goals, tolerance, trade-offs, reactions)
- Multiple stakeholders, goals, times, levels (utility)
- Constantly changing over time
- Very sensitive to changing individual life circumstances, unexpected life events, markets (ups-downs)
- The “subject/client” itself is changing as well: Individuals’ tolerance, appetite and understanding of risk change constantly (education, experience, life events, a financial crisis,...)
- Model assumptions... over long horizons
- The advice itself may create an important feedback loop!
- Difficult to capture complete picture – optimization is very sensitive to these assumptions and definitions



Adoption of Risk-Based Toolkit...

Must be careful on borrowing from banking and institutional applications

- For market risk, typically, short term
 - Banking: 1 day (trading) or 1-2 weeks (regulation)
 - Asset Management: longer, e.g. 1 month
- Used for controls/limits, trading, hedging, optimization
- Objective related to maximize risk adjusted returns (perhaps relative to a benchmark for Asset Management)

For wealth management... this is different...



It's all About Risk... ... but Risk is Not a Number....

Risk in wealth management involves more than just analyzing a portfolio

- Entire view of a family's wealth... not only a single investment portfolio
- Multiple portfolios and accounts... and tax implications...
- A client's (family's) risk capacity/tolerance/appetite
- Multiple goals and timelines... over long horizons (5, 10, 20, 50 years)
 - Accumulation (pre-retirement) and decumulation (post-retirement) periods
- Scale... if you are a successful advisor, you likely have a large number of clients that you want to manage efficiently...

It's *all* about Risk... .. but Risk is Not a Number....

In financial advice... Risk is a "Story"

*A powerful communication tool constantly
guiding the narrative and the engagement*

The Wealth Management Risk Cycle



Investor's Risk Profile

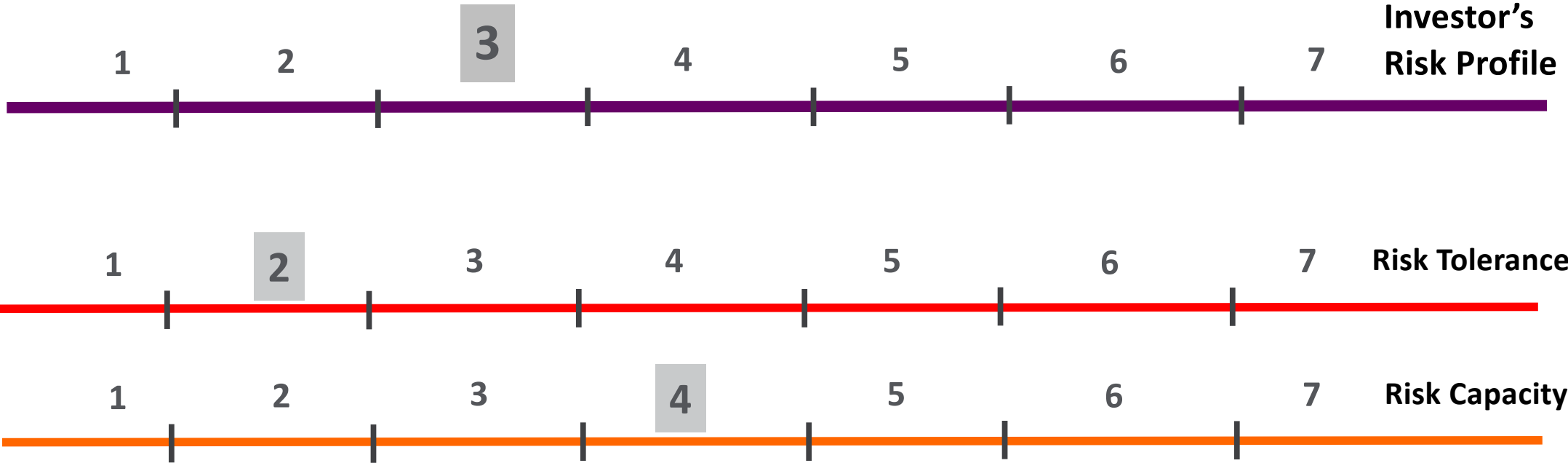
Multiple metrics are needed to characterize an “Investor’s Risk”

- Risk Capacity
- Risk Tolerance / Risk Appetite
- Financial knowledge
- Information appetite

Risk return trade-off / risk aversion

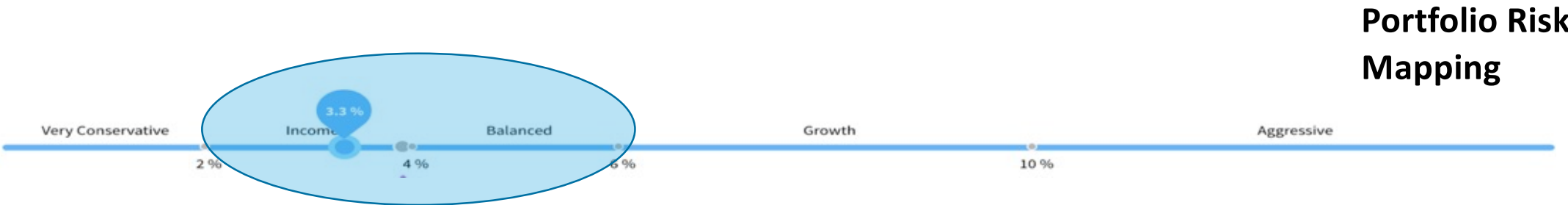
Tools include: Behavioural Finance and Psychometrics

Investor's Risk Profile



Household/Family: risks profiles defined for the entire household and members

Aligning Risks across the Cycle



Goals & Risk

Goals reflect an investor's (individual or household) needs, wants, wishes and dreams

Typical measures for future short-term portfolios (large) losses do not relate directly to goals

- VaR, expected shortfall, volatility, drawdown...

Goal-based Risk → the possibility of not achieving these goal(s) in the future, how far we will be, and the severity/consequences (for a given portfolio or investment strategy over time)

Relevant metrics

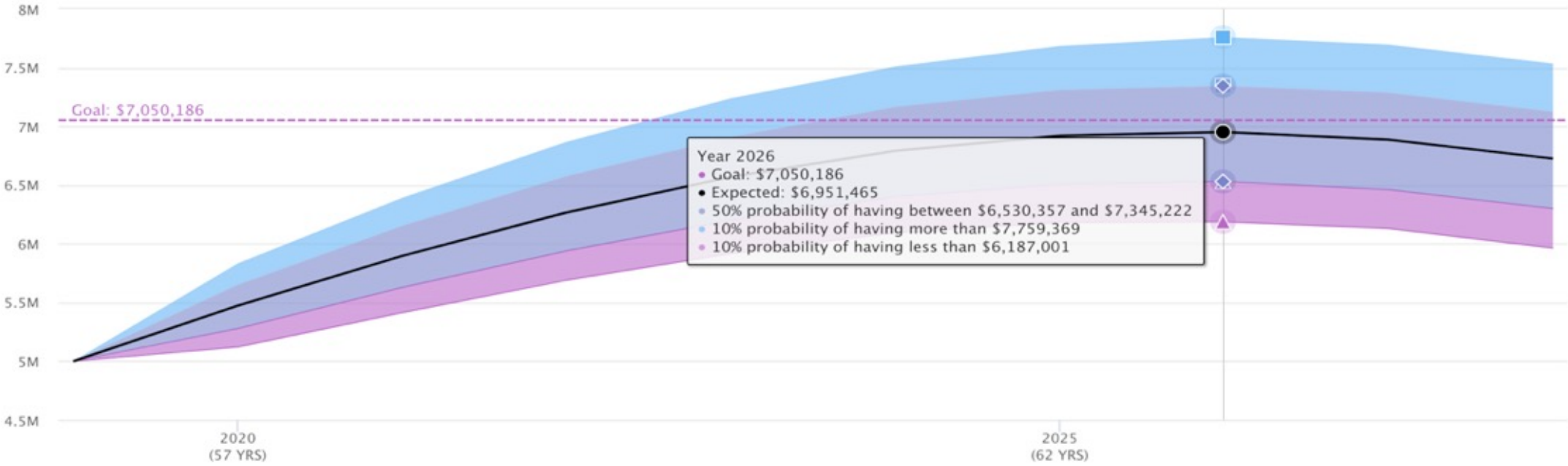
- Probability of meeting goal(s)
- Distance to meet goal (for a given strategy and scenarios)
- Expected shortfall (conditional on not meeting goal)
- Trade-offs between competing goals

Long-Term Wealth Simulation (Accumulation)

Projected Wealth Simulation

At **65** years old, you expect to have accumulated **\$6,725,456**

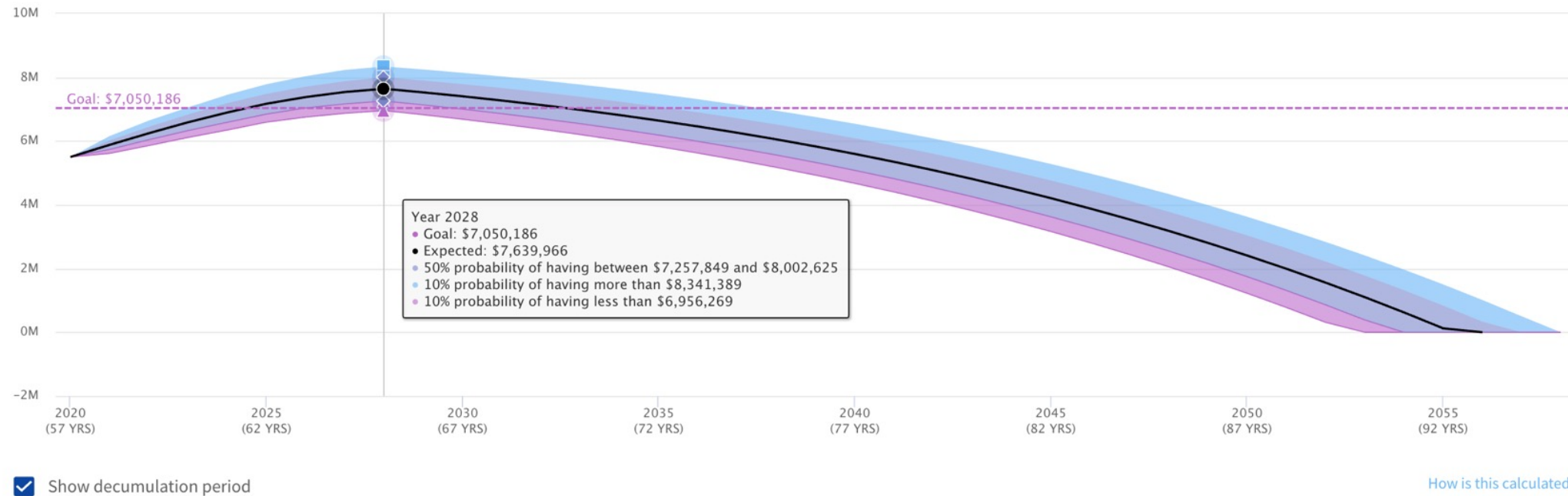
- Goal: Retire at 65
- \$200,000/year until age 95
 - High likelihood of achieving (90%)



Long-Term Wealth Simulation (Retirement Income & Decumulation)



Projected Wealth Simulation



Investment Plans, Mandates, IPSs

In practice, this needs to be realistic

- Multiple goals and timelines
- Multiple actors: different risk profiles and timelines
- Multiple sources of funding (different rules, taxes)

Solution must be actionable: easy to execute, track, and communicate

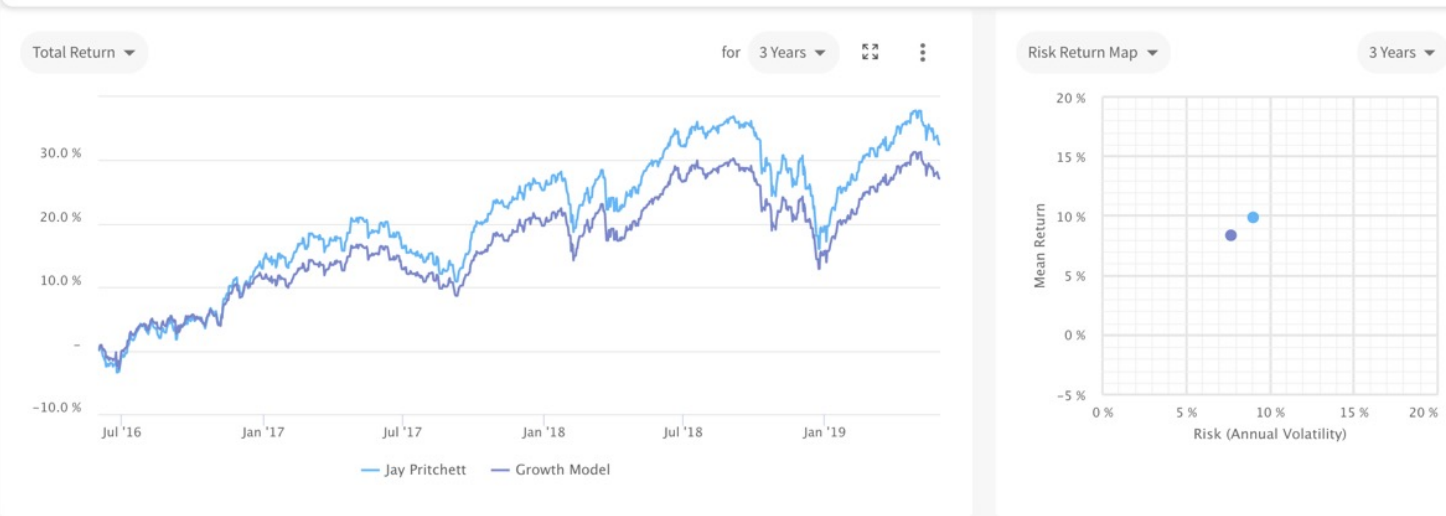
- Multiple mandates/sub-mandates acting together
- Funded through multiple accounts and financial vehicles (e.g. trusts and insurance)

Constructing & Rebalancing Portfolios

IPS – Model Portfolio’s Risk



Actual Portfolio’s Risk

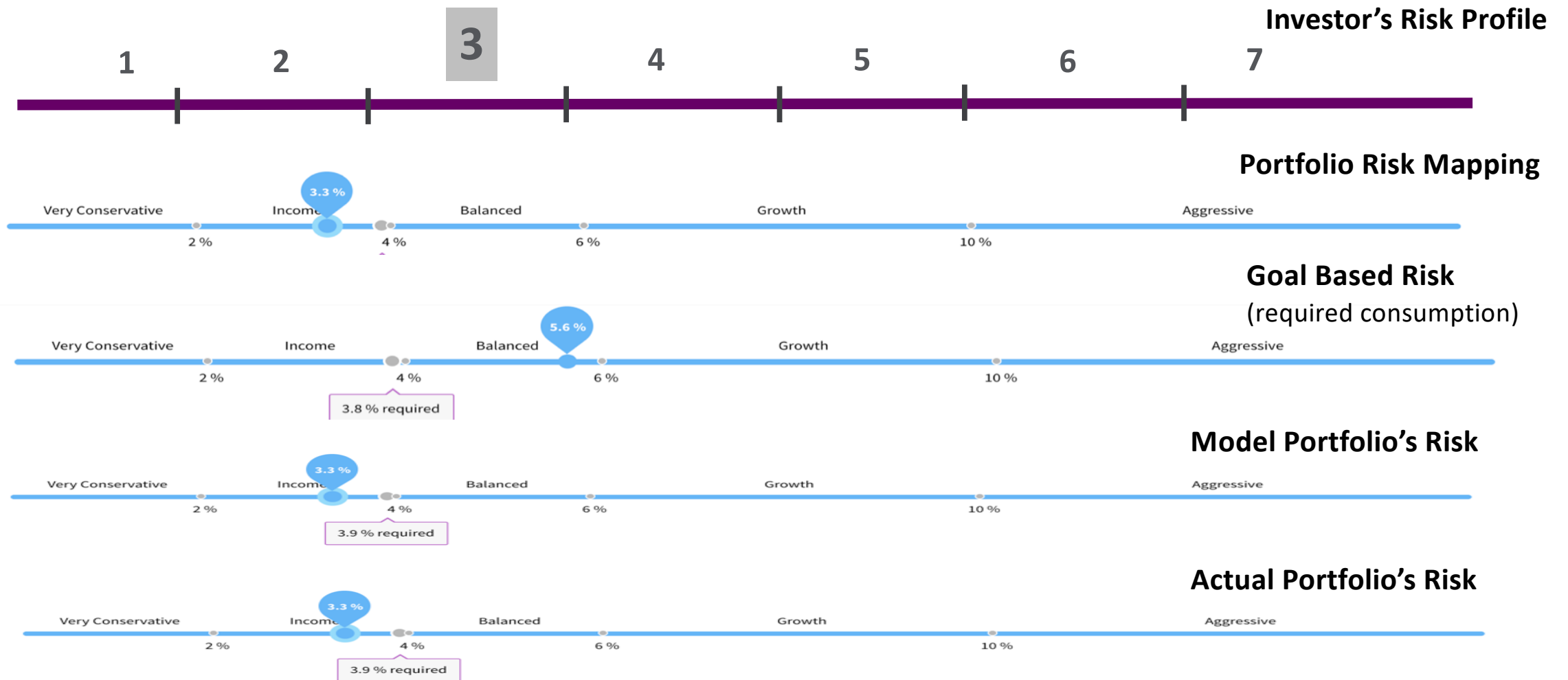


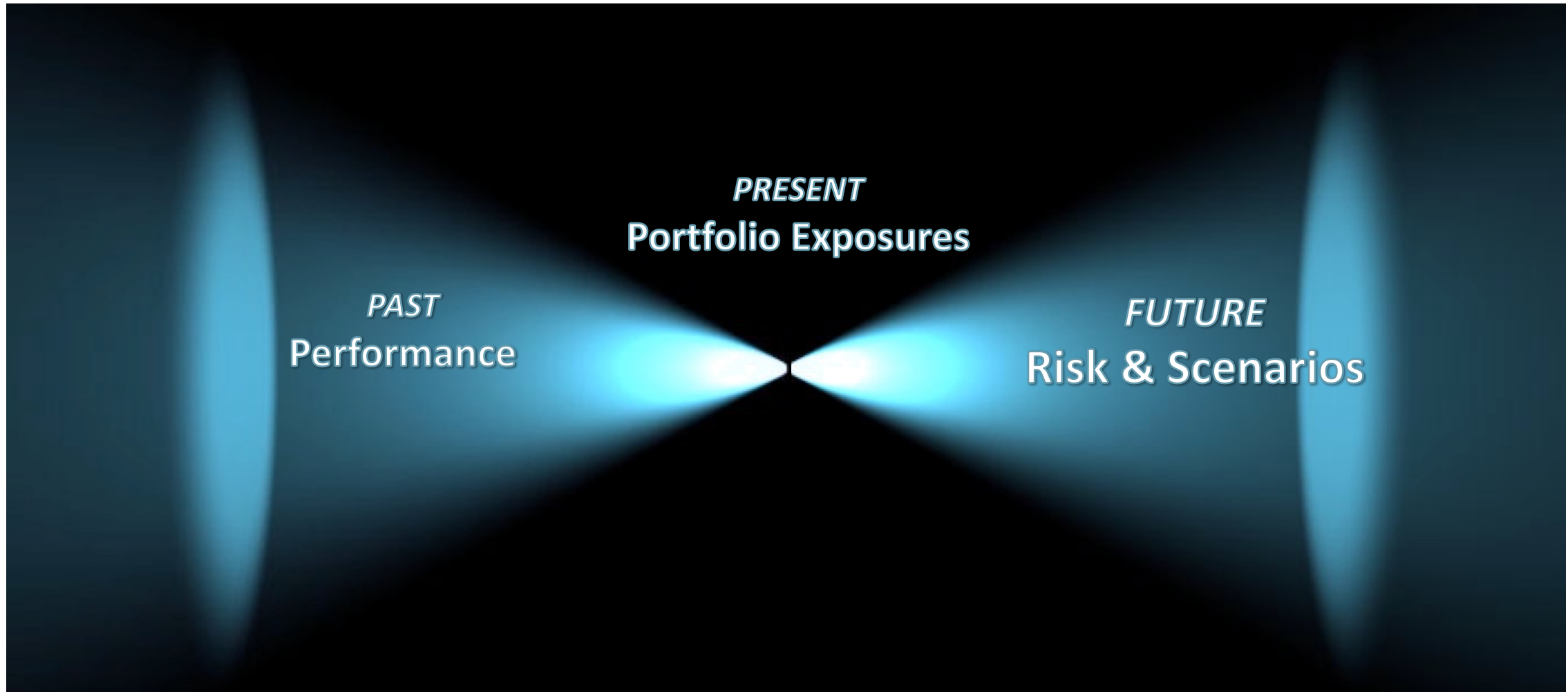
Search for data containing...

Portfolio View

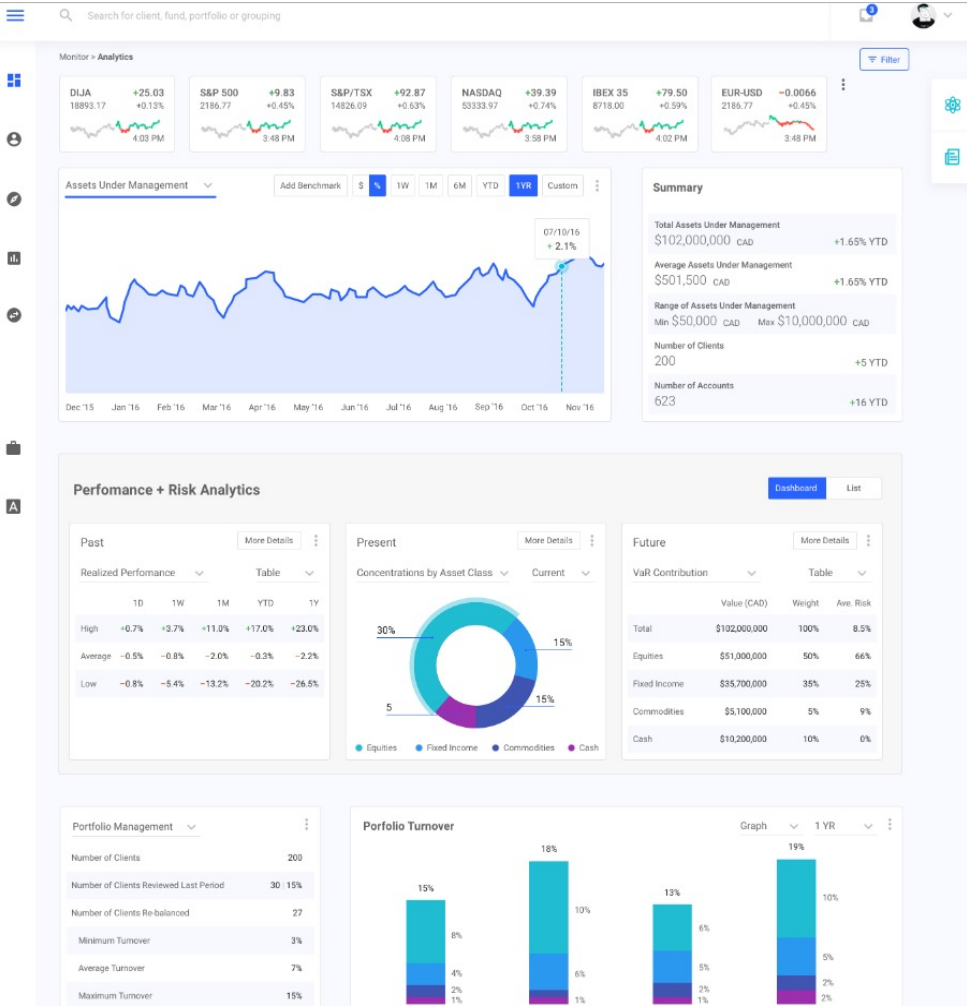
Security Name	Return (YtD)	Return (1Y)	Return (3Y)	Volatility (3Y)	VaR (90%)	Drawdown (3Y)	% of Portfolio			
							Total	Cash & Cash Equivalent	Equity	Fixed Income
Jay Pritchett	10.9 %	2.3 %	9.6 %	9.9 %	5.2 %	13.6 %	100.0 %	8.8 %	90.0 %	1.2 %
Growth Model	10.0 %	2.5 %	8.4 %	8.6 %	4.4 %	12.0 %	100.0 %	2.8 %	77.1 %	20.1 %

Aligning Risks across the Cycle – Tracking Mandates & Portfolios





Monitoring Portfolios: Exposures, Performance, Risk



Tracking Portfolios... and understanding causes:

- Exposures: slice & dice
- Performance attribution
- Risk contributions
- Scenario Analysis
- Risk factor analysis and decomposition
- Cashflow forecasts

The Wealth Management Risk Cycle



Wealth Management Risk... and Performance

Behavioural

- Risk Tolerance
- Risk Capacity
- Risk Appetite



- ***Exposures***
- ***Performance attribution***
- ***Portfolio Risk & diversification***
 - Market Risk (short & long-horizon)
 - Credit Risk
 - Liquidity Risk
- ***Stress Scenarios***

ALM/Household Treasury

- Gap Risk
- Shortfall
- Prob of achieving goal (distance to Goal)

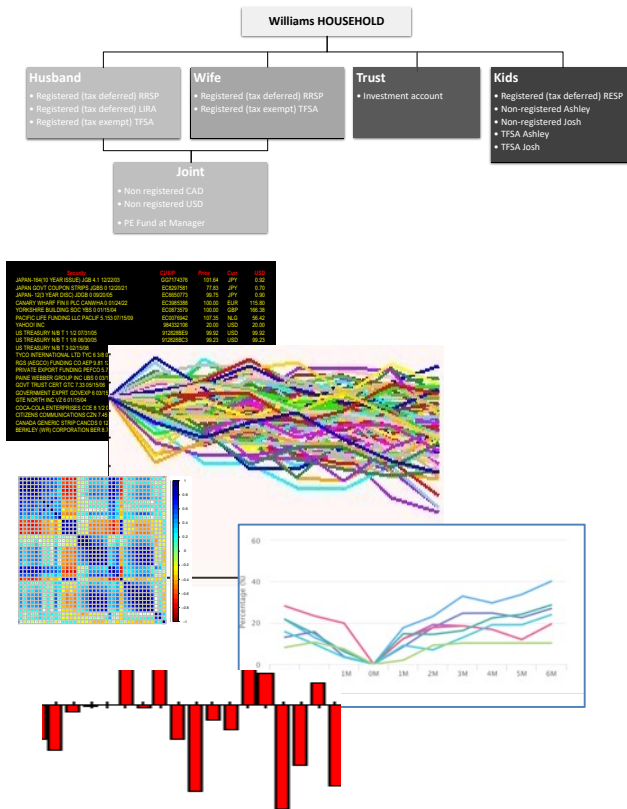
Wealth Portfolio Optimization: Efficient Portfolio Manufacturing at Scale!



Objective: provide personalized, and high-touch portfolio investment programs for 100s or 1000s of clients in an efficient manner

- Understand the entire book of business
 - Pro-actively (instead of reactively) address which clients
 - Require more attention
 - Can take advantage of an opportunity
 - Are more affected by a given market event...
- Dynamic, interactive engagement with a given client to define what is important and understand trade-offs

The Mother-of-All Portfolio Optimization in Wealth Management



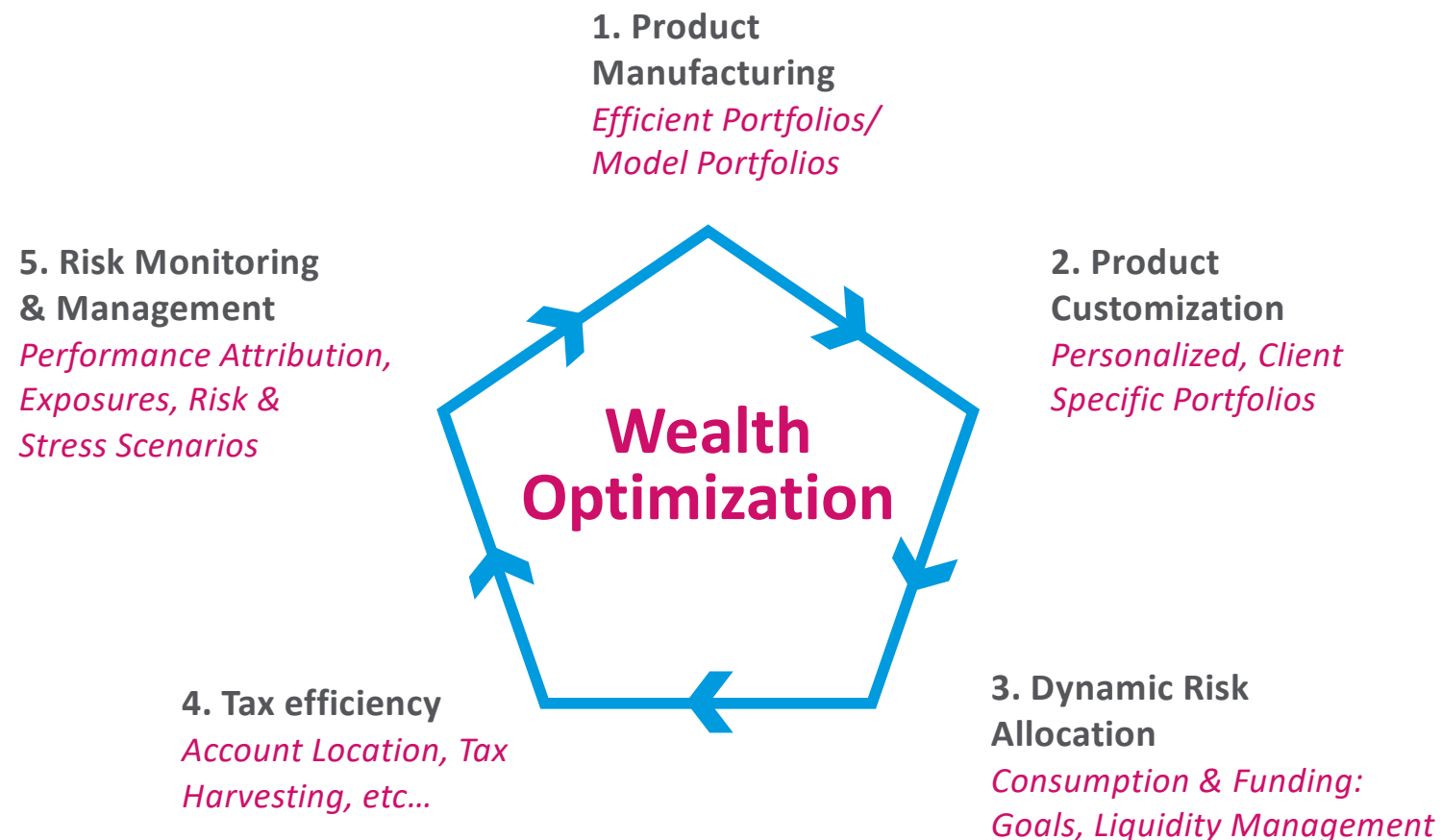
Find the “Optimal” overall portfolio strategy for the Household

- Maximizes multi-criteria utility function
 - Multiple goals over time: inflows and outflows; some terminal wealth (or multiple) on a long horizon
 - Accounting for taxes, risk profiles, stochastic markets
 - Rich scenario set (multi-factor forecasting model)
 - Takes best advantage of investment universe available
 - Complex constraints: consistent with multiple client risk/investment preferences, liquidity, compliance/regulatory (tax)

Output

- Asset (risk-factor) allocation now
 - Across all members (legal-entities) and accounts (location)
- Dynamic allocation over time (long horizon)

Quantitative Portfolio Manufacturing Process



Goal: to use the best financial optimization tools to break the process into a set of steps:

*Effective,
Manageable,
Repeatable,
and Scalable.*

Quantitative Portfolio Manufacturing Process

1. Product Manufacturing

*Efficient Portfolios/
Model Portfolios*



Efficient Portfolios & Model Portfolios

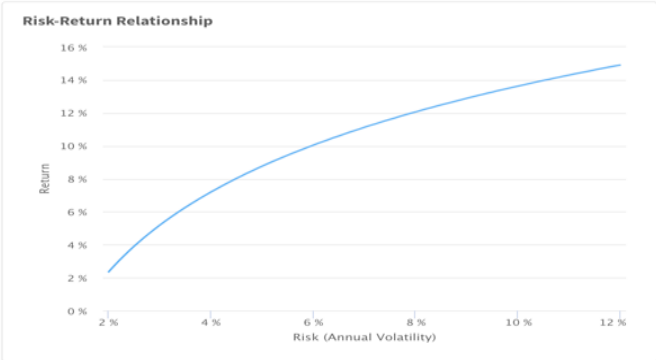
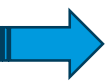
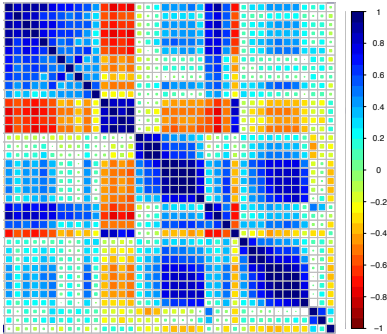
Construct set of optimal model portfolios or investment programs, based on available investment vehicles and expertise (available for all clients... segmented)

- Define *Investment Universe* (opportunities)
- Asset allocation, risk factor allocation, diversification
- Advanced optimization toolkit: e.g. Black-Litterman, Bayesian models, etc...

Output: full set(s) of “efficient” **general Model Portfolios**

Investment Universe

Security	DUIS	Price	Curr	USD
JAPAN 164(10 YEAR ISSUE) JGB 4.1 12/22/03	GG7174376	101.64	JPY	0.92
JAPAN GOVT COUPON STRIPS JGBS 0 12/20/21	EC2627591	77.83	JPY	0.70
JAPAN 12(3 YEAR DISC) JDBG 0 09/20/05	EC5850773	99.75	JPY	0.90
CANARY WHARF FIN II PLC CANWHA 0 01/24/22	EC3885388	100.00	EUR	115.80
YORKSHIRE BUILDING SOC YBS 0 01/15/04	EC0873579	100.00	GBP	166.38
PACIFIC LIFE FUNDING LLC PACLIF 5.153 07/15/09	EC0078942	107.35	NLG	56.42
YAHOO! INC	984332106	20.00	USD	20.00
US TREASURY NB T 1 1/2 07/31/05	912826659	99.92	USD	99.92
US TREASURY NB T 1 1/8 06/30/05	912828823	99.23	USD	99.23
US TREASURY NB T 3/02/15/08	912828477	100.59	USD	100.59
TYCO INTERNATIONAL LTD TYC 6 3/8 01/15/04	9021204F1	85.00	USD	85.00
RGS (AEGOO) FUNDING CO AEP 9.81 12/07/21	749550A49	133.36	USD	133.36
PRIVATE EXPORT FUNDING PEFCO 5.73 01/15/04	742651C06	103.89	USD	103.89
PAINE WEBBER GROUP INC US 0 03/15/05	695634K04	100.00	USD	100.00
GOVT TRUST CERT GTC 7.33 05/15/06	383751A42	100.00	USD	100.00
GOVERNMENT EXPRT SOU/EP 5 03/15/05	383751A55	104.40	USD	104.40
GTE NORTH INC VZ 5 01/15/04	382337A29	103.64	USD	103.64
COCA-COLA ENTERPRISES CCE 8 1/2 02/01/22	191219A99	130.44	USD	130.44
CITIZENS COMMUNICATIONS CZN 7.45 01/15/04	177342H45	101.80	USD	101.80
CANADA GENERIC STRIP CANCDS 0 12/01/21	135062V08	34.22	CAD	25.46
BERKLEY (WR) CORPORATION BER 8.7 01/01/22	084423A06	112.05	USD	112.05



Quantitative Portfolio Manufacturing Process

1. Product Manufacturing
*Efficient Portfolios/
Model Portfolios*

2. Product Customization
Personalized, Client Specific Portfolios

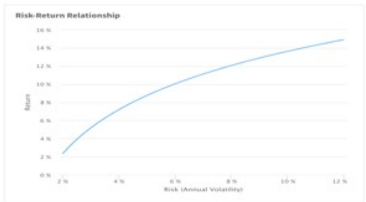
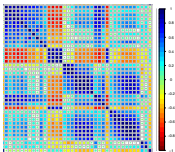


Customized Client Model Portfolios

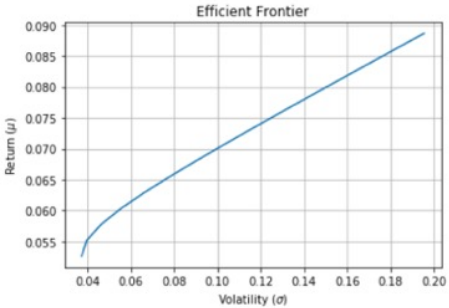
Adjust model portfolios to create a specific personalized subset for each individual client

- Additional Input: client specific constraints, investment preferences
- Use of advanced optimization toolkit for asset/risk factor allocation, diversification
- Output: subset of adjusted **client-specific “efficient” Model Portfolios**

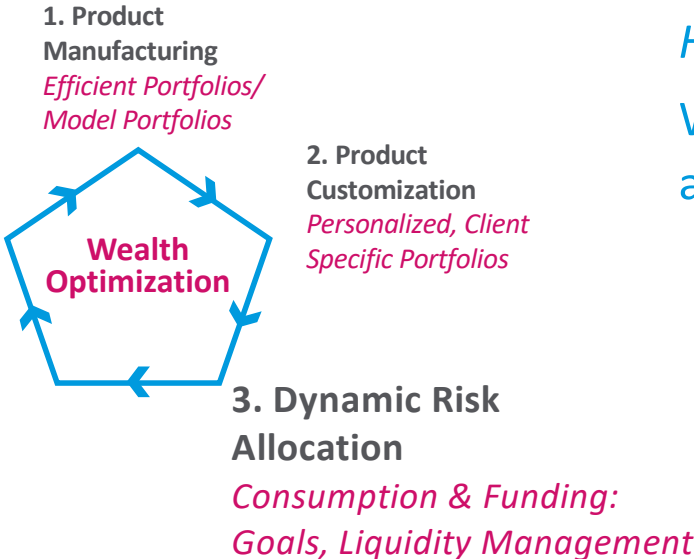
Security	COOP	Price	Qty	USD
JAPAN GOVT BOND 05/20/2023	0017428	101.64	10	0.00
JAPAN GOVT BOND 05/20/2021	0028076	101.64	10	0.00
JAPAN GOVT BOND 05/20/2028	0028077	101.64	10	0.00
CANARY REAFF FAL PLC CANARY 05/20/22	0028078	101.64	10	0.00
TOMORROW'S BOND CO 05/20/2028	0028079	101.64	10	0.00
PACIFIC LIFE FUNDING LLC PCLF 5/20/2028	0028080	101.64	10	0.00
SPAC INC	0028081	101.64	10	0.00
US TREASURY NB 1 1/2 07/2025	0028082	101.64	10	0.00
US TREASURY NB 1 1/2 07/2026	0028083	101.64	10	0.00
US TREASURY NB 1 1/2 07/2027	0028084	101.64	10	0.00
TECH INTERNATIONAL LTD 5/20/2028	0028085	101.64	10	0.00
ROD JACOBZ FUNDING CO AP 5/20/2021	0028086	101.64	10	0.00
WINDLE EIGHT FUNDING CO 5/20/2028	0028087	101.64	10	0.00
WINDLE EIGHT FUNDING CO 5/20/2028	0028088	101.64	10	0.00
GOVT TRUST CERT 5/20/2028	0028089	101.64	10	0.00
GOVERNMENT EMPLOY GROUP 05/20/2028	0028090	101.64	10	0.00
GTB NORTH INC 05/20/2028	0028091	101.64	10	0.00
CITIZEN COMMUNICATIONS CORP 5/20/2028	0028092	101.64	10	0.00
CANARY REAFF FAL PLC CANARY 05/20/22	0028093	101.64	10	0.00
REPLEY PPA COMPANY 05/20/2022	0028094	101.64	10	0.00



Client Specific Model Portfolios

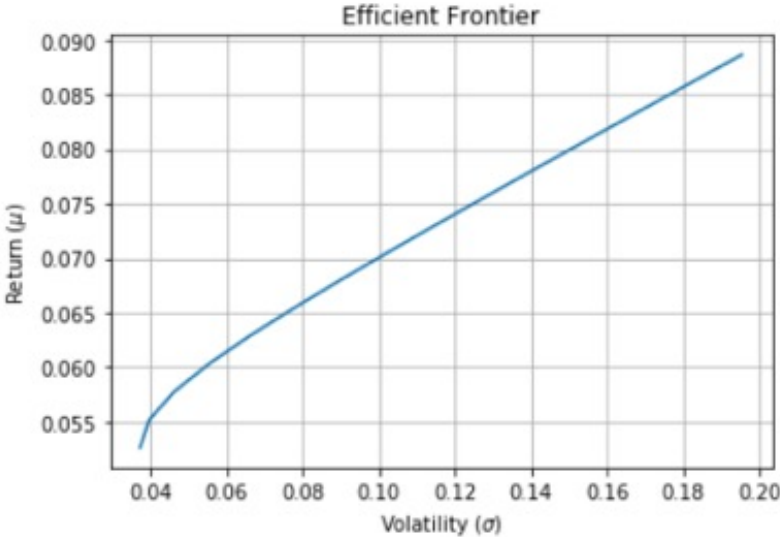


Quantitative Portfolio Manufacturing Process

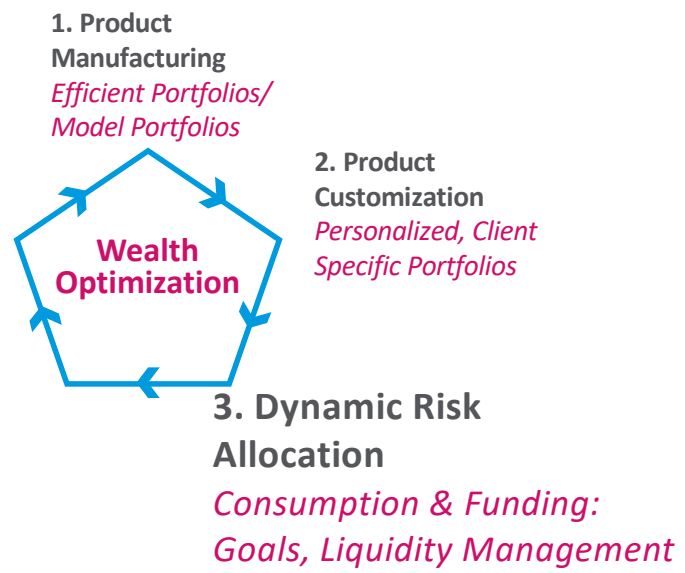


How do we pick how many portfolios and “Lambdas”?

Which portfolios or asset/risk factor allocations do we invest in now... and over time (rebalancing)



Quantitative Portfolio Manufacturing Process

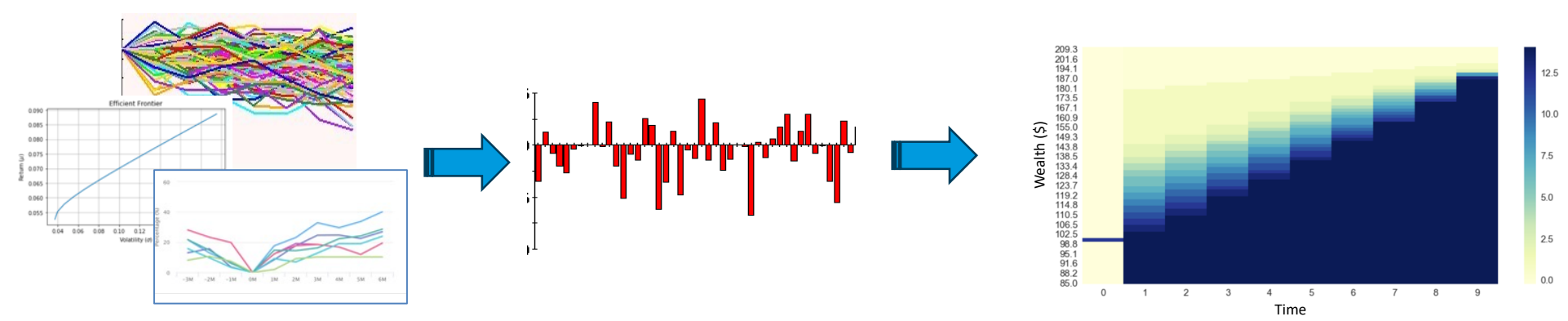


Dynamic Portfolio Investment Strategies: meet goals and manage liquidity (long horizons, 10-50 years)

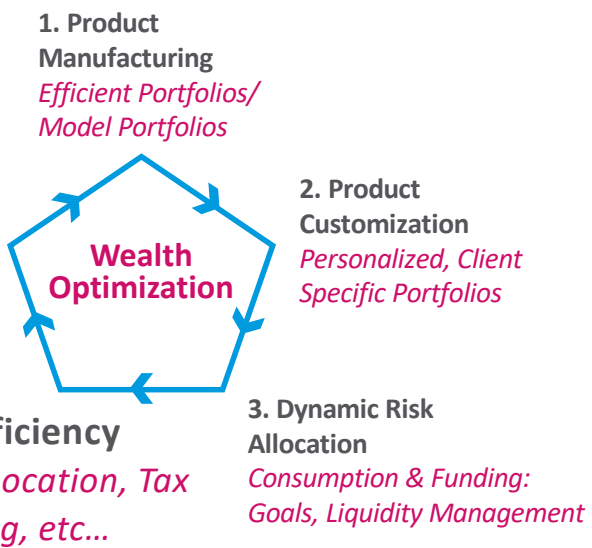
Goal-based Wealth Management (*Household ALM*)

- Includes accumulation, liquidity management (inflows, outflows, capital calls, etc...) and decumulation/wealth transition (post retirement)
- **Stochastic Dynamic Portfolio Optimization**: dynamic programming and machine learning tools (Reinforcement Learning, Neural Networks)

Output: **dynamic allocation** (of efficient portfolios) of over time based on goals, sensitivities and what-if analysis



Quantitative Portfolio Manufacturing Process

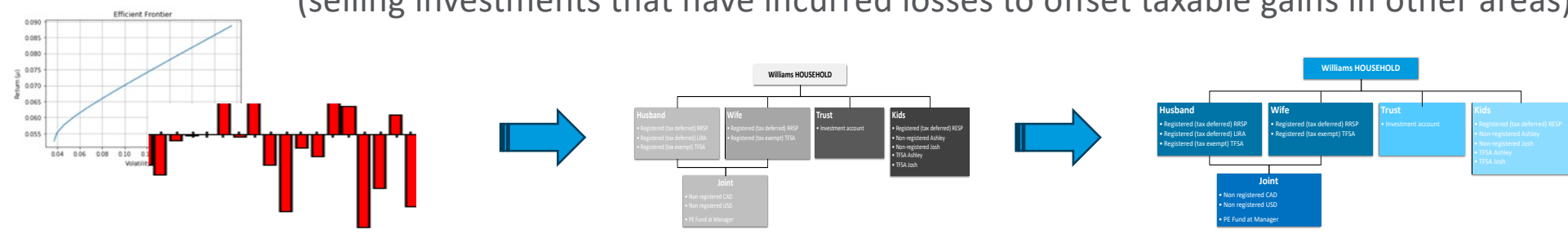


Optimize for Tax Efficiency (*maximize after-tax risk-adjusted returns*)

Detailed tax optimization to adjust portfolio location and sources of income streams

- Account for: different tax-advantaged accounts, marginal tax rates for different products, income sources, and legal entities, the timing of realized gains)
- Optimization model incorporates details on:
 - Income thresholds, tax brackets, deduction limitations, specific rules related to tax-advantaged accounts, tax lots, etc..
 - Tax Rate Functions applicable to different income levels and types of income (e.g., ordinary income vs. capital gains)

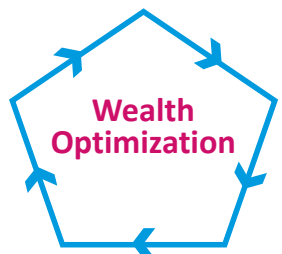
Output: client and account location, income adjusted plan, tactical tax harvesting (selling investments that have incurred losses to offset taxable gains in other areas).



Quantitative Portfolio Manufacturing Process

5. Risk Monitoring & Management
Performance Attrib., Exposures, Risk & Stress Scenarios

1. Product Manufacturing
Efficient Portfolios/ Model Portfolios



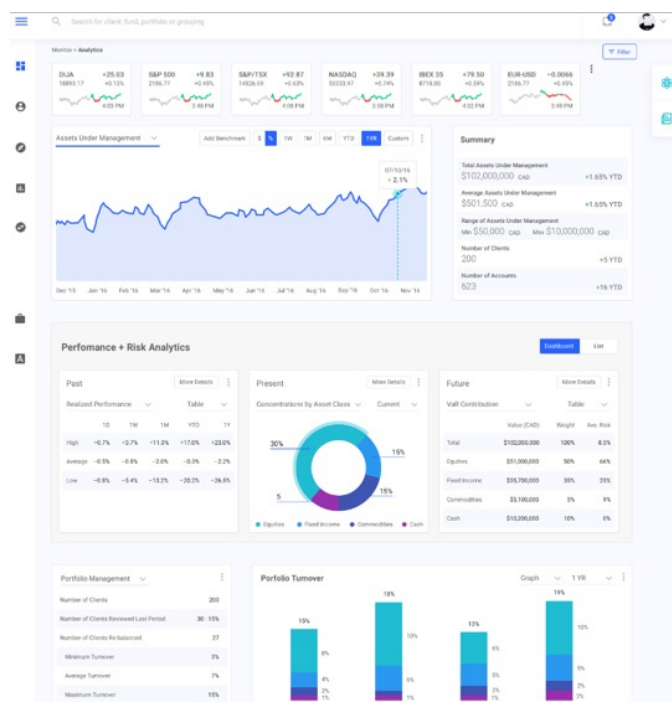
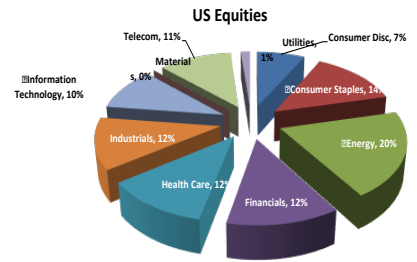
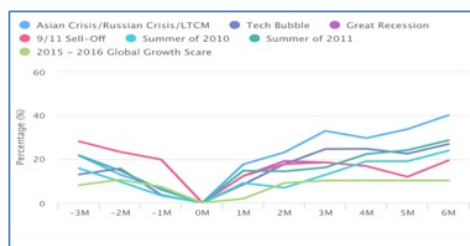
2. Product Customization
Personalized, Client Specific Portfolios

4. Tax efficiency
Account Location, Tax Harvesting, etc...

3. Dynamic Risk Allocation
Consumption & Funding: Goals, Liquidity Management

Actively Monitor and Understand Exposures, Performance and Risk

- Compliance with IPSs and client periodic reviews
- Changes in: markets, client's life circumstances, goals, regulation, ...
- What if – available new funds or investment opportunities
- Scenario analysis



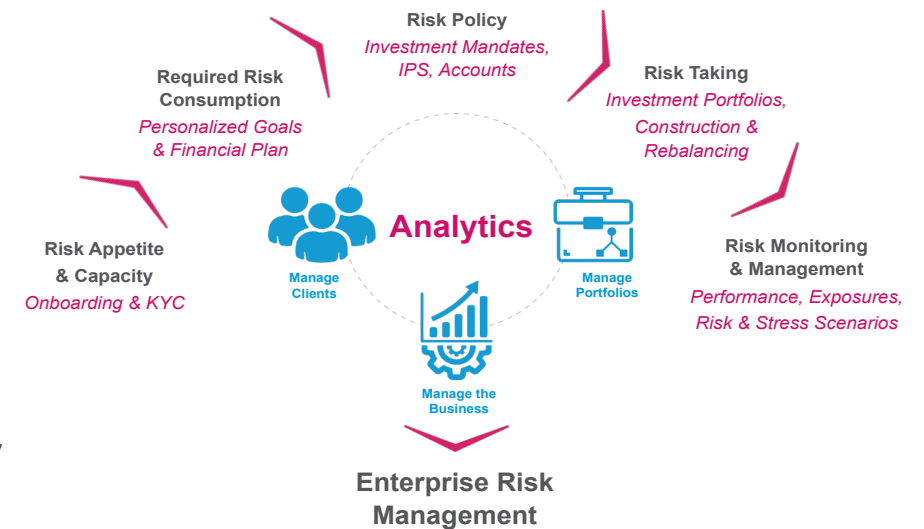
Analytics Across The Wealth Management Risk Cycle

The modern Wealth Management analytics toolkit integrates

- Behavioural Finance
- Goal-Based Planning
- Modern Portfolio Theory, Portfolio Optimization
- Risk Measurement/Management Tools
- Data science, marketing

Analytics

- OR tools: decision making and planning under uncertainty
- AI / Machine Learning
- Computational Finance and economics



... Specifically: a long-term investment focus

Example: Goal-Based Wealth Management

Goals-based wealth management (GBWM):

Management of an investor's portfolios

with a view to meeting long-term financial goals

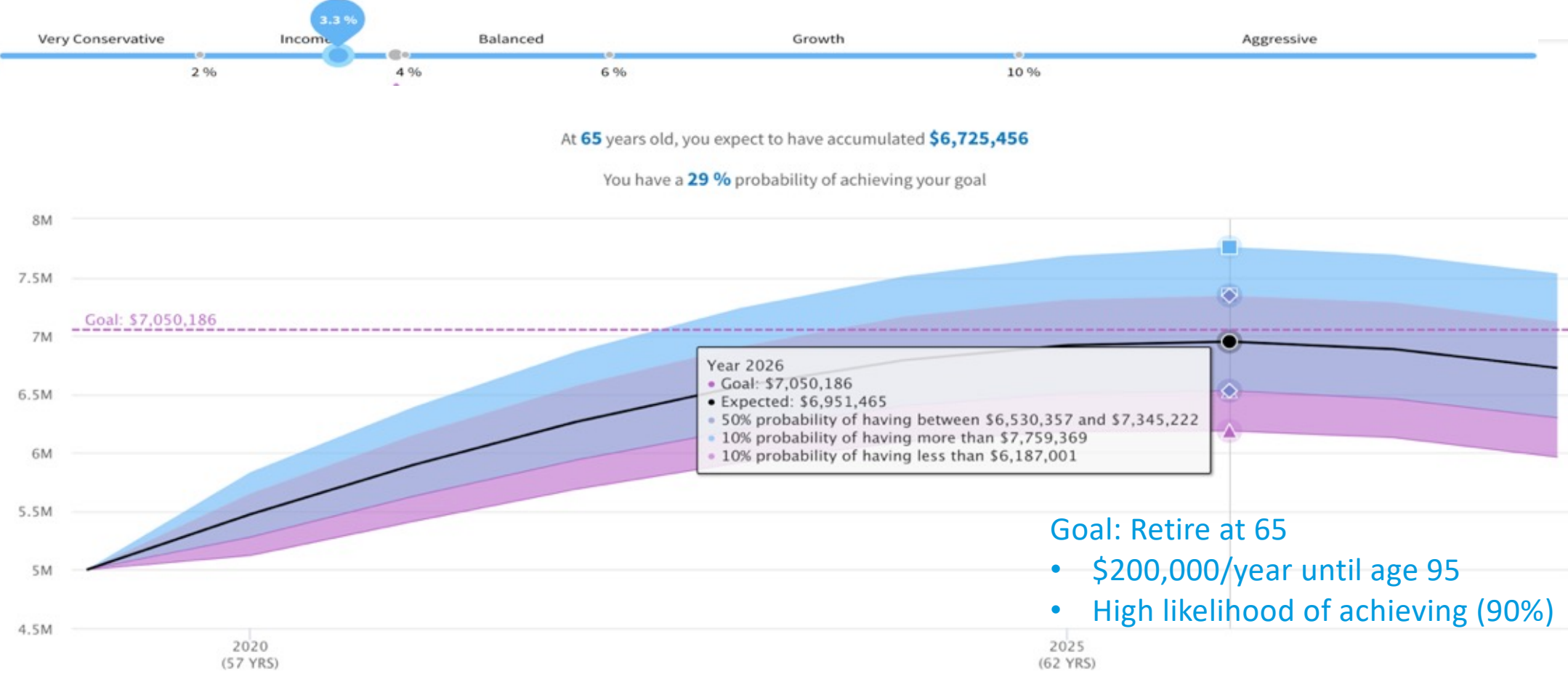
(as opposed to only optimizing a risk-return tradeoff)

In the end:

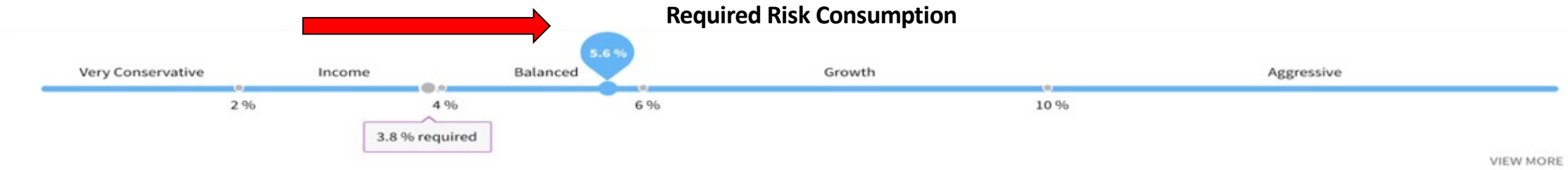
Why are we saving money? ... to invest it.

Why are we investing? ... to fulfill some important goals in the future

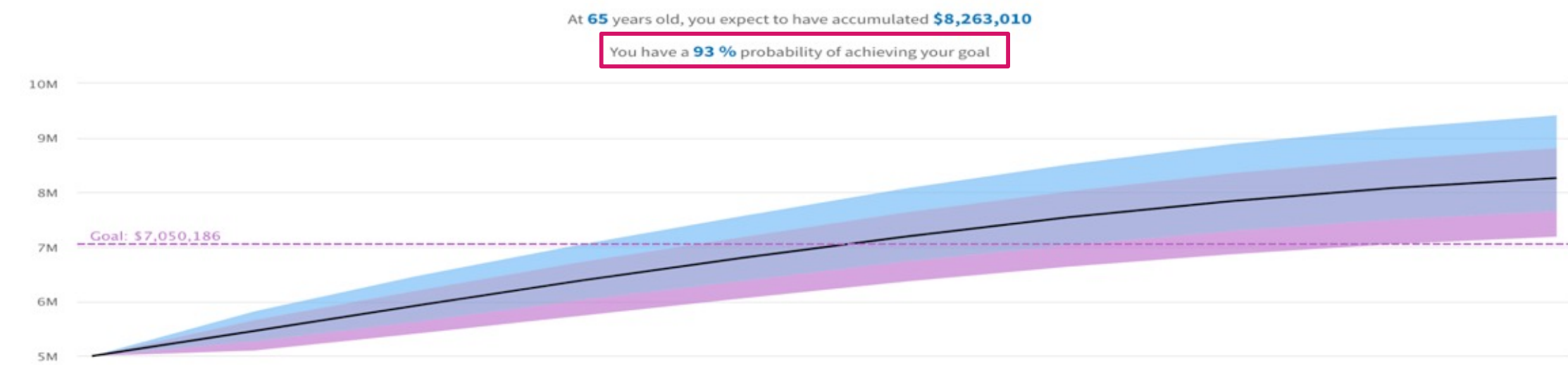
GBWM – Wealth Simulation



GBWM- Wealth Simulation



Projected Wealth Simulation

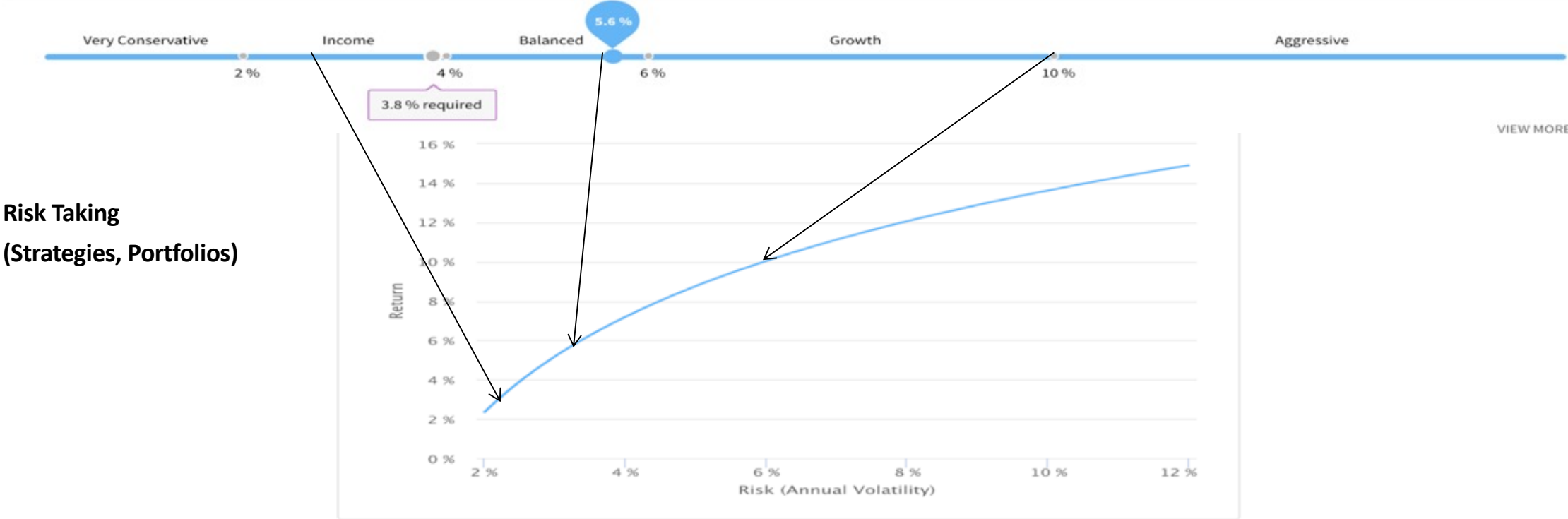


Integrating GBWM, MPT & Risk

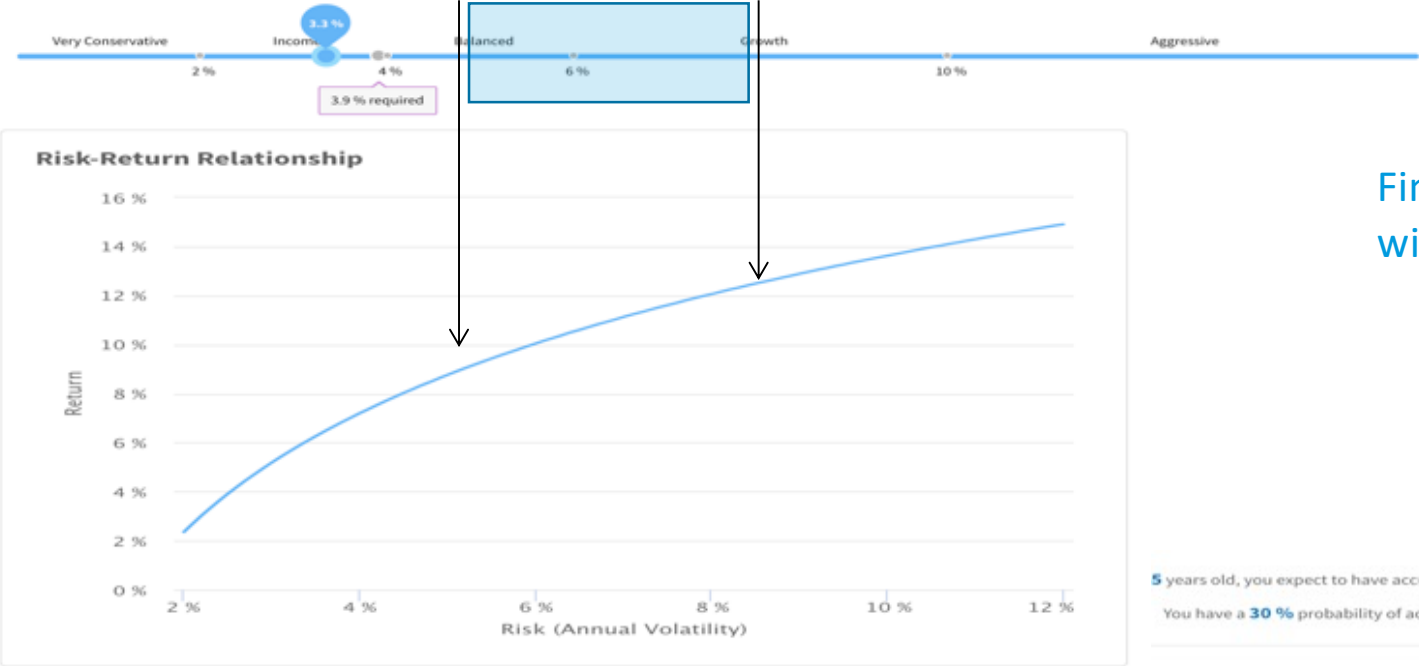


- We can consistently combine:
 - Goal Based investment planning
 - Modern Portfolio Theory, Portfolio Optimization tools
 - Psychometrics and behavioural finance
- Focus on (long-term) risk measures related to:
 - Probability of achieving goal(s)
 - Distance (shortfall) to achieving goal(s)
- Create explicit links to portfolio risk measures (volatility, VaR, drawdown, etc...)
- Optimal solution: portfolio(s) to choose now.... + the strategy over time

Integrating GBWM, MPT & Risk

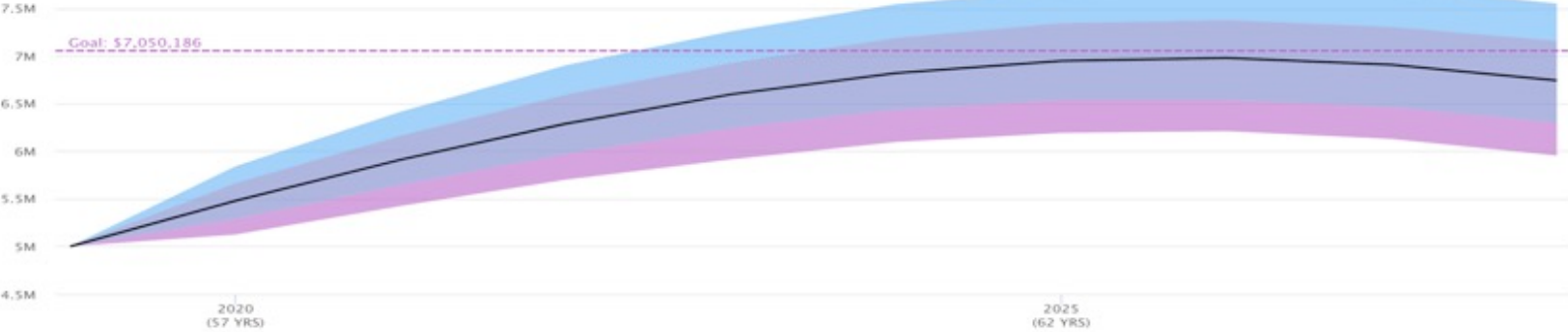


Integrating GBWM, MPT & Risk



Find Portfolios that achieve goal with at least 90% probability

5 years old, you expect to have accumulated **\$6,741,528**
 You have a **30%** probability of achieving your goal



Goal-Based Portfolio Optimization

Goal Based Portfolio Optimization – intuitive and actionable tool for financial advisors

- Maximize the likelihood of achieving the goal (or set of goals)
- Minimize the distance to achieving the goal (e.g. mean squared errors, shortfall)

Key insight: integrate MPT by choosing the portfolio set on the efficient frontier – splitting:

- Optimal asset allocation, and
- Required risk taking to achieve goal

Example – Das et al. (Markowitz Price, JoIM 2019)

- Static (constant risk) solution
- Dynamic goal-based portfolios (using stochastic dynamic programming)
- Trading off Multiple goals
- Dynamic portfolios via Reinforcement Learning

Other examples: Dixon & Halperin (Quants of the year 2022), Forsyth et al....

Dynamic Portfolio Optimization for GBWM

The static case is easy to understand and solve – but not “dynamically” optimal

- Implementations in practice are done period by period, in a simplistic manner
- Widespread rule-of-thumb approaches, such as “target-date” portfolios

Dynamic programming solutions outperform static solutions and rules-of-thumb

- Discrete-time dynamic programming approach
 - Fast and simple to implement
 - Flexible: handle periodic infusions/withdrawals, bankruptcy, multiple goals at different times
 - Insights into real-life implementation strategy, effects of changing environment over time
- More general Machine Learning tools (RL and NN)

Remember... Key insight: splitting

- Optimal asset allocation, and
- Required dynamic risk taking over time to achieve goal

Dynamic Portfolio Optimization for GBWM – Key Features

1. Objective Function

- The standard dynamic programming approach: **Max Expected Utility** (consumption over time & final wealth)

In GBWM, we can alternatively use more intuitive objective functions (e.g. Das et al, Forsyth et al):

- Maximize Probability of achieving the goal:

$$\max Pr \{W(T) > G\}$$

- Minimize the Distance to achieving the goal (or to underperforming goal):

$$\min E \{ ||W(T) - G || _ \} \text{ (typically the 2-norm)}$$

Dynamic Portfolio Optimization for GBWM – Key Features

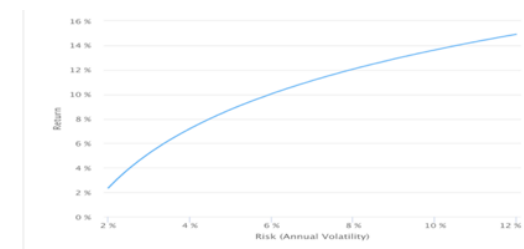
1. Objective Function (e.g. Das et al, Forsyth et al)

- Maximize probability of achieving the goal: $\max Pr \{W(T) > G\}$
- Minimize the Distance to achieving the goal (or to underperforming goal): $\min E \{ ||W(T) - G || \}$

2. Decisions, $A(t)$: *allocations* from a finite set of possible portfolios available at each $t = 0, 1, 2, \dots, T - 1$

- Most people solve directly the full asset allocation (n asset classes or large- n instruments) at every step
 - This can be a difficult, multi-dimensional problem
- Instead, decision variables $A(t)$ are discretized into a finite sub-set
 - Computationally efficient
 - Consistent with advisor-investor problem, portfolios can be chosen from a set of available *Model Portfolios*

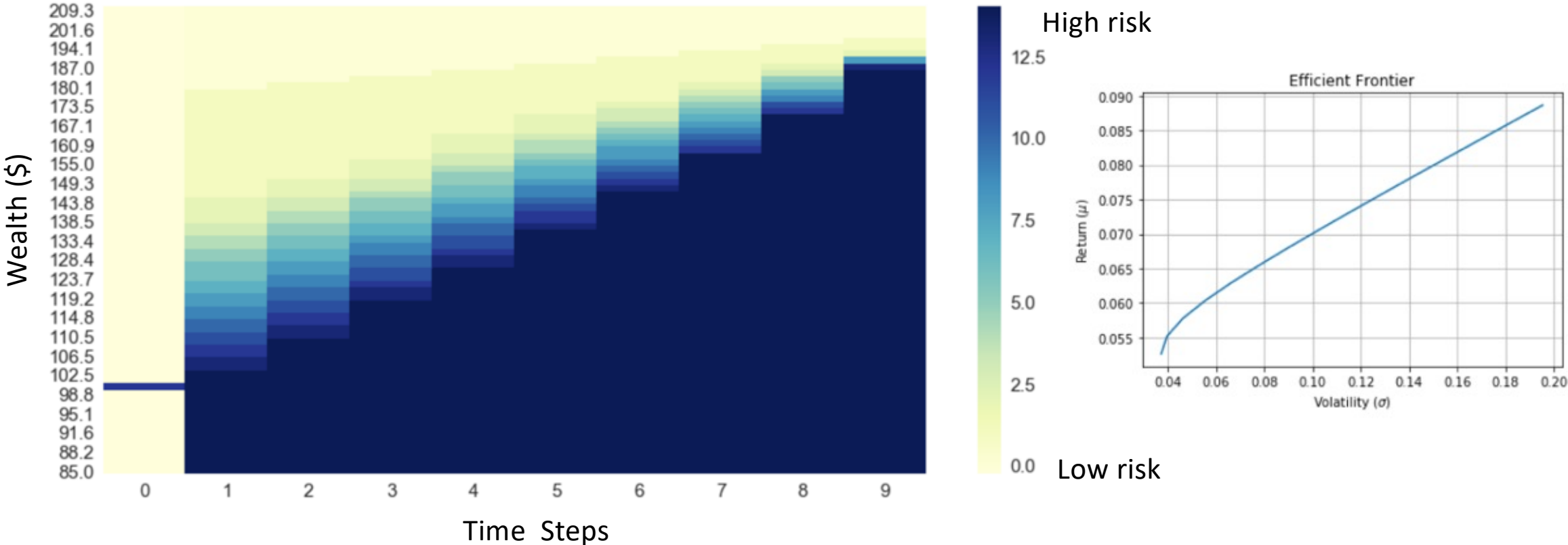
3. Efficient portfolios: Portfolios $A(t)$ in the efficient frontier – consistent with MPT



Dynamic Portfolio Optimization for GBWM – Key Features

1. Objective Function (e.g. Das et al, Forsyth et al)
 - Maximize probability of achieving the goal: $\max Pr \{W(T) > G\}$
 - Minimize the “Distance” to achieving goal (or to underperforming goal): $\min E \{ ||W(T) - G || \}$
2. Decisions, $A(t)$: *allocations* from a finite set of possible portfolios available at each $t = 0, 1, 2, \dots, T - 1$
 - Decision variables are discretized into a finite sub-set (not solving directly full asset allocation for every step)
3. Efficient portfolios: typically, the portfolios $A(t)$ are in the efficient frontier – consistent with MPT
4. Solution: function over the 2-D discretized grid in t and $W(t)$
 - **Dynamic programming** (backward recursion): most effective when wealth process $W(t)$ is tractable (e.g. GBM), as we need to calculate conditional probabilities
 - **Reinforcement learning** (RL) or **Neural Networks**: applicable to a general setting and non-parametric, data-driven, processes (e.g. Das et al, Forsyth et. Al, Halperin et al)

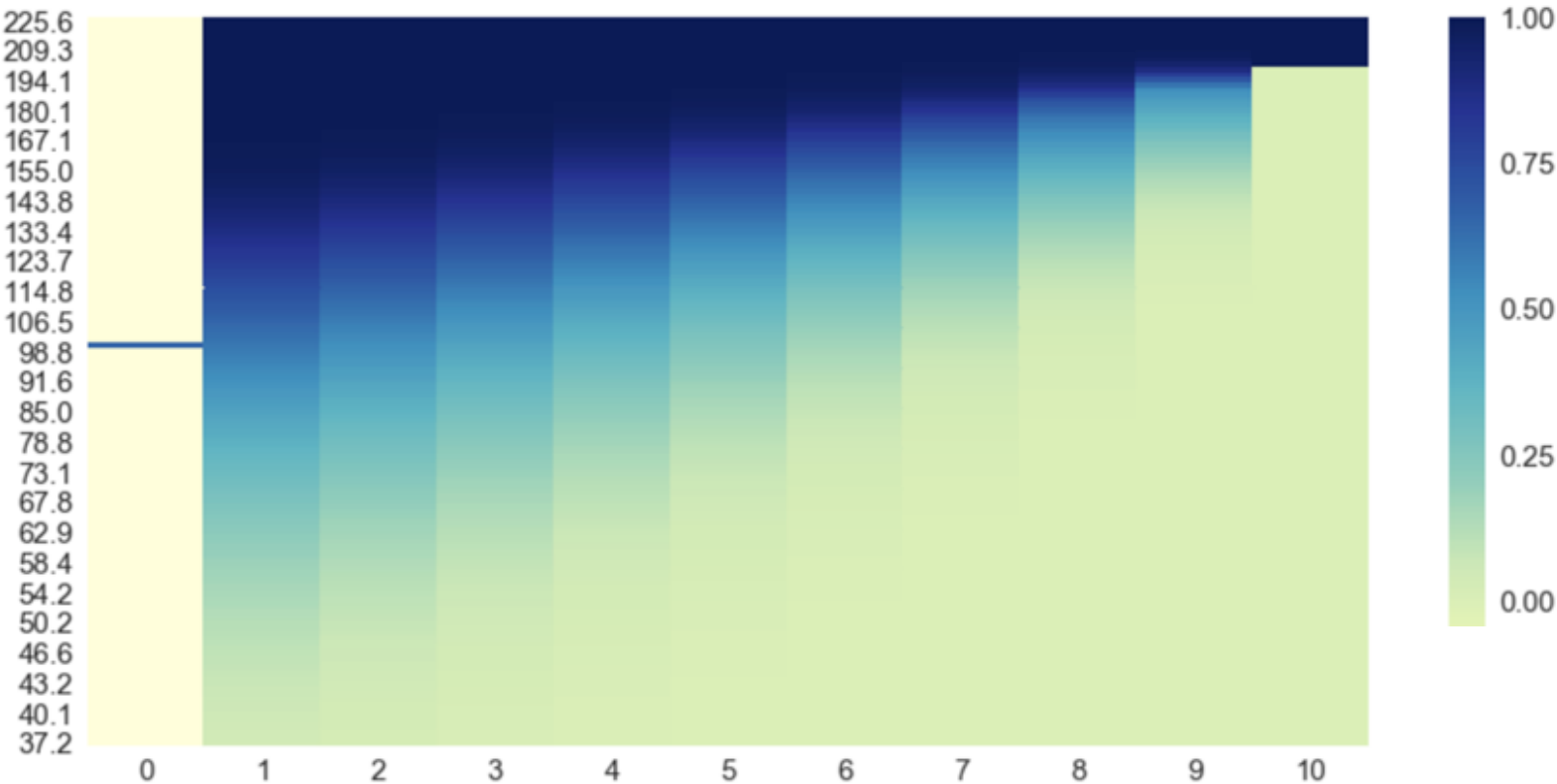
Dynamic Portfolio Optimization – Example (Das et al.)



Optimal dynamic portfolio strategy – grid corresponding to each wealth node and time

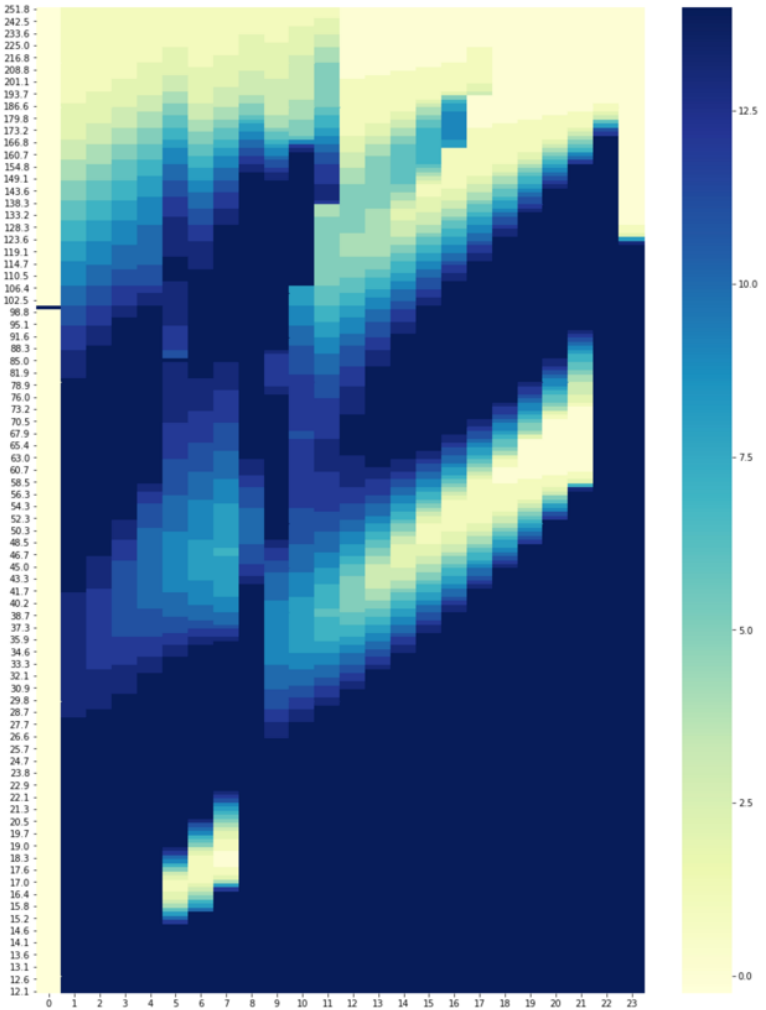
Wealth Goal: $G = \$200$ after 10 periods

Dynamic Portfolio Optimization – Example



Optimal probability (of reaching the goal), at each wealth node and time
Wealth Goal: $G = \$200$ after 10 periods

Dynamic Portfolio Optimization – Example



Example: Grid of optimal portfolios for multiple goals at different times

- Multi-criteria optimization using a utility function (weighting function for multiple goals)

Modelling Dynamic GBWM

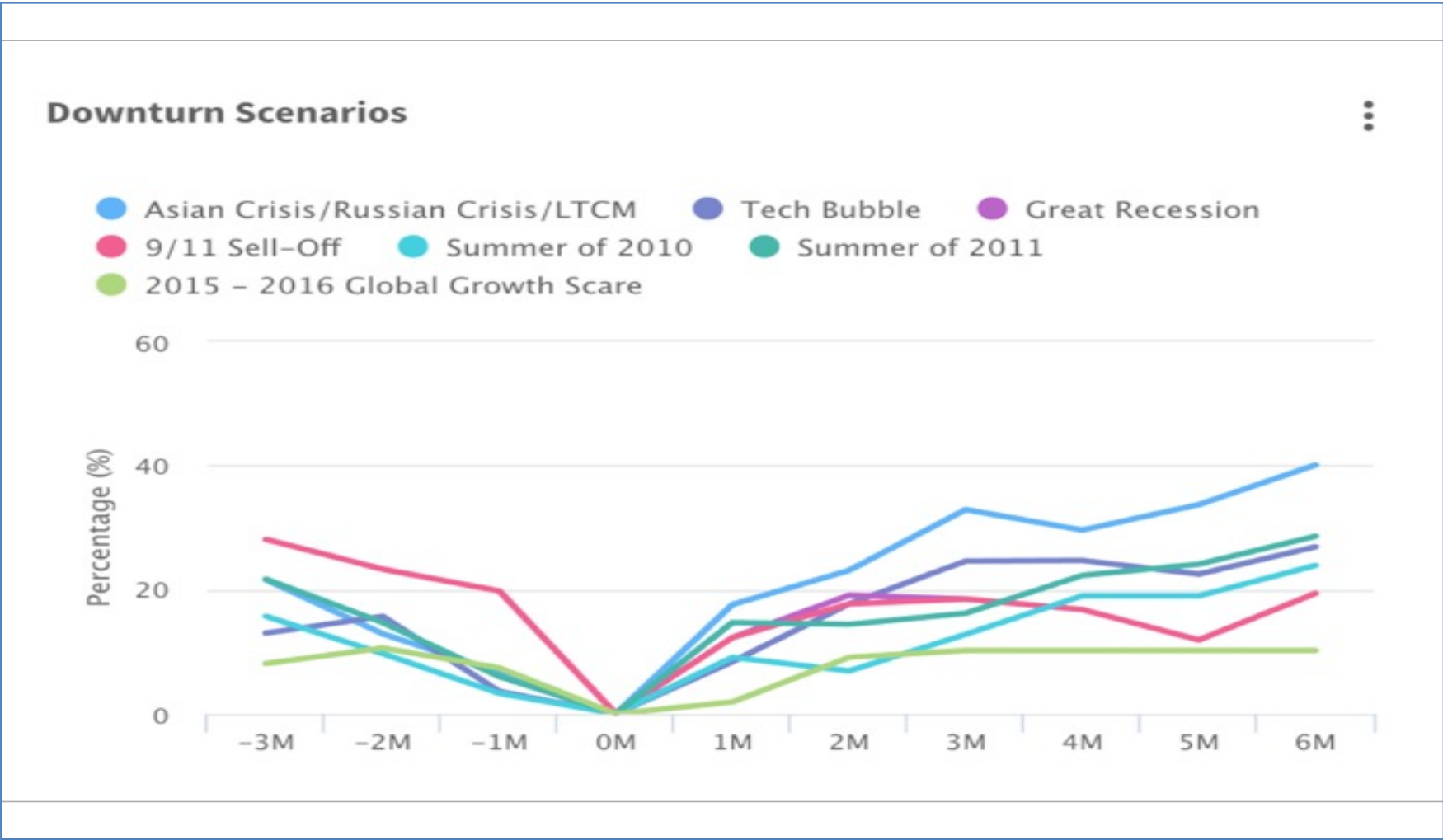
The dynamic setting further allows to make the problem more realistic

- Handle multiple (competing) goals at different points in in time: e.g. buying a cottage in 2 years, vs. retirement vs. leaving inheritance
 - Handling different priorities and level of importance (via utility function)
- Goals at different level of the family hierarchy and multiple ways of funding
- Uncertain cashflows (inflows and outflows)
- Realistic financial details: e.g. tax assumptions
- Realistic economic model and stress scenarios...

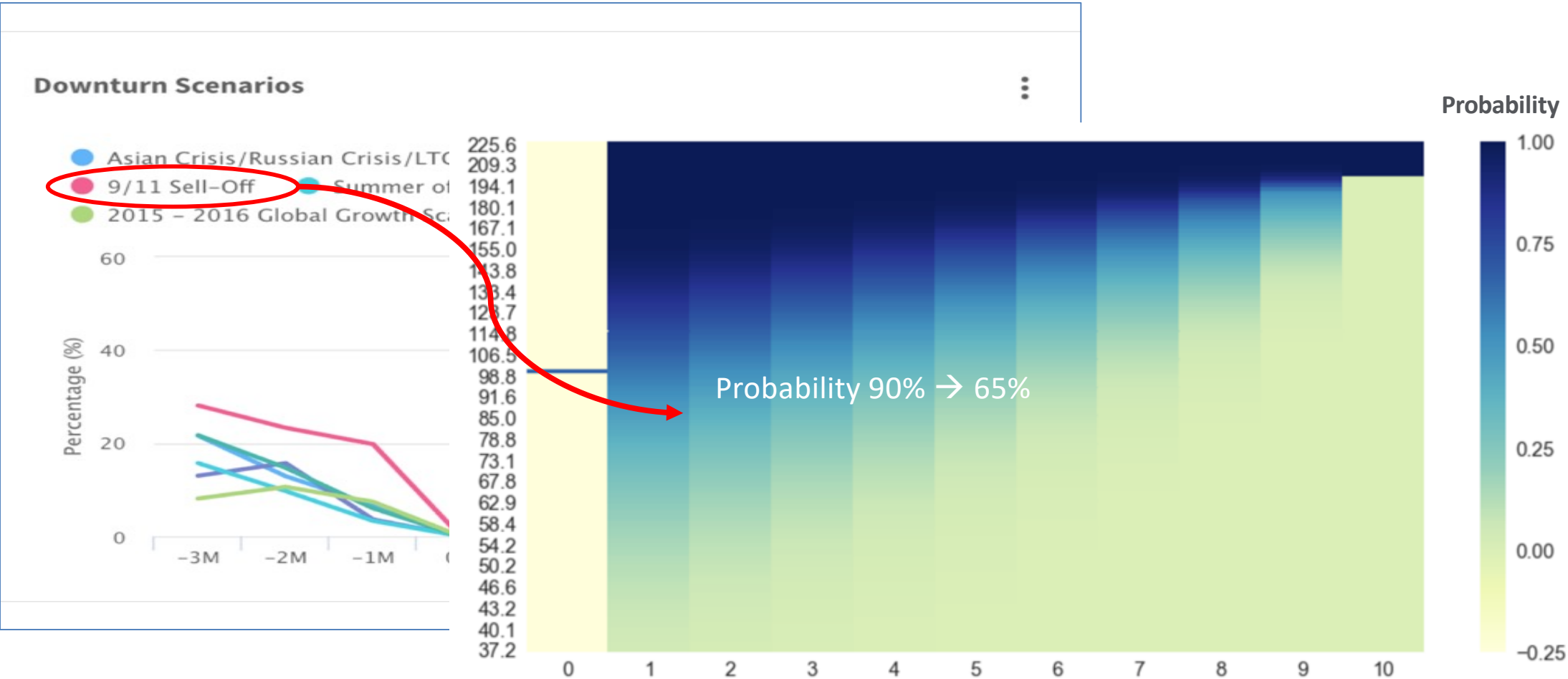
The optimization setting also allows us solve for

- Sensitivities, what-if analyses, trade-offs
- Inverse problem: Find most likely scenario(s) or actions that may affect our goals – severity, timing...

Overlaying Historical Scenarios



Example: Overlaying Historical Scenarios & Drawdowns



Dynamic Portfolio Optimization for GBWM

What's the big deal?


- Most practitioners solve the planning problem over ONE SCENARIO... or 3 scenarios 😊
 - Good as a simple Base to understand the problem, but not realistic and does not incorporate risk!
 - Perform perhaps some stress testing
- Some perform a simplistic MC simulation with limited (simplified) asset classes and may test static portfolios or some simple strategies
- MPT-based single-step portfolio strategies that are rebalanced periodically
- Some attempts at dynamic optimization with direct asset allocation – lead to only simplistic goals, simplistic portfolios (small number of theoretical asset classes) which are difficult to implement and computationally intensive

ML tools such as Reinforcement Learning and NN are particularly well-suited for this problem and have now also opened the possibilities – computationally intensive and complex to implement

In Practice... Financial Risk for Humans

Interactive engagement and coaching – multiple goals & questions the client/investor relates to

- How did the likelihood of achieving the goal changed with a recent drawdown?
- What's the max drawdown I can take? When do I need to worry?
- If I can't meet goal precisely, how far are we? What are my trade-offs between multiple goals?
- How else can I fund the plan?
- When can I de-risk portfolio? How much can I take out and not affect goal?



**Big Data, analytics, AI
and other digital technologies
will not eliminate
the need for the human touch...**

THANK YOU !

Dr. Dan Rosen

CEO *d1g1t*

dan.rosen@d1g1t.com